

# **New Jersey Math Outcomes Analysis 2015/16**

**Grade Levels: 3, 4, 5**  
**ST Math Program: Gen-4**  
**Analysis Type: Three-Year**  
**Treatment-Years: 2013/14, 2014/15, 2015/16**  
**Baseline-Year: 2012/13**  
**Subgroup: All**

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## Abstract

This analysis covers all grades using ST Math in New Jersey in 2015/16. It identifies those grades with nominal or better implementation of the ST Math program, and matches them to randomly selected, similar math-performance, comparison grades. The nominal ST Math users are an aggregation of 13 grades, consisting of grades 3, 4, and 5 at 5 schools, with an average baseline of 85% in Met or Exceeded Expectations proficiency levels (refer to Figures 2 and 3 to see how your schools compare to those analyzed in this report). They were matched to 13 similar, randomly selected control grades at 13 schools that never used ST Math. Grade-wise growth in math proficiency was evaluated (i.e. growth in same grade, same school, from 2012/13 to 2015/16) on the percentage proficient, scale scores, and Z-scores of the scale scores (see Section 3.1). Grades 3, 4, and 5 aggregated showed an ST Math effect of 3.82 points at the Met or Exceeded Expectations levels, 5.97 points at the Proficient Level, and Z-score of 0.14.

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# 1 Introduction

## 1.1 Background

This is a quasi-experimental analysis at the grade-mean level. Entire grades represent the units of analysis, and outcome measures are the 3-year changes in grade-mean PARCC Met or Exceeded Expectations percentages. The treatment grades used the ST Math program for 3 years, beginning in the 2013/14 school year. The study hypothesis is treatment grades using ST Math will outperform similar matched control grades, using their “business as usual” conditions of instructional content and professional development. The control grades were selected to have similar demographic and math attributes to the treatment grades during the baseline year (2012/13), and did not use ST Math in 2013/14, 2014/15, and 2015/16. The treatment grades’ selection pool was all schools using ST Math in grades 3, 4, and 5 in New Jersey. The control grades’ pool was all schools not using ST Math in grades 3, 4, and 5 in New Jersey. This study method measures effectiveness of the ST Math program when nominally implemented.

## 1.2 Program Description

The ST Math program is a supplemental math program covering grade-level New Jersey math standards. The ST Math content consists of visual representations of math standards, concepts, and procedures, presented to students as “Puzzles” of virtual manipulatives, with which they interact to pose solutions. Each time the student poses a solution, the computer visually animates the Puzzle, diagram, or symbols to show why the posed solution correctly solves, or why it does not solve, the math problem (puzzle). The Puzzles are arranged into sequential groups, called “Levels”. To proceed to the next Level in sequence, the student needs to master his/her current Level. Mastering a Level requires solving 100% of the math problems, or Puzzles correctly. In this way, the program is self-paced. Students must correctly solve approximately 4-12 Puzzles, with only 1 failure and retry allowed, to proceed. Levels are sequenced together into Games and, again, the student must master each Game to get to the next Game in sequence. Games are sequenced into “Learning Objectives” (e.g. ‘Fractions Concepts’). The ST Math curriculum of approximately 20-25 Learning Objectives can be rearranged in a year-long, grade-level syllabus to match district math pacing through the school year.

The Puzzles typically start with concrete representations of the math, without abstract symbols, math vocabulary, or even English words. Gradually, through subsequent Levels or Games, abstractions are introduced. For example, a Puzzle might start with “n” green blocks on the screen, and then at a subsequent Level may represent the quantity with the numeral for “n” (no green blocks anymore). In this way, three things are accomplished: i) language proficiency prerequisites to engage with the program are minimal, ii) non-mathematical distractions (e.g. back-stories for word problems) are minimized or eliminated – thereby reducing load on working memory, and iii) the actual math in the problem can be represented clearly, simply, and unambiguously.

Besides the self-paced progress made by students in their one-to-one environment, the program is designed to be referenced by teachers during their regular math instruction. It is supplemental to core or basal math instruction and instructional materials. As the great majority of grade-level math standards are covered in the ST Math digital curriculum, completion of 100% of the entire ST Math curriculum (i.e. completing every Game) is required to cover all grade-level math standards.

Teachers receive initial training, either face to face or through self-guided online instruction. The training covers account startup, as well as math learning and growth mindset goals, the pedagogical

approach to learning in a visual experiential game, monitoring and intervention of the student 1:1 game play, and connecting of ST Math content to classroom content and pacing.

To achieve nominal progress through the program, there is a time-on-task requirement. While student progress rates through the program vary, MIND Research Institute has found that consistent application of 90 minutes per week throughout the school year is sufficient to get most students through at least half of the ST Math Learning Objectives. Students are recommended to use the program in school for at least two 45-minute sessions per week, or 90 minutes per week, over about 35 weeks. Analyses of ST Math usage have shown that consistently following this schedule throughout the school year is usually sufficient to achieve 50% or more Progress through ST Math content. Progress is a percentage of ST Math content coverage, and is defined as Levels completed by the student, divided by the total number of Levels in the curriculum. In addition, MIND’s historical analyses have shown that it is necessary to complete at least 50% of the program in order to expect significantly higher performance compared to non-users.

## 2 Data Collection

Since this analysis uses grades as the unit of analysis, and states publish grade-mean state standardized test scores, the data for student math outcomes is collected from each state education agency’s research files (retrieved from state websites). The school-level demographic data is also collected from the MDR (Market Data Retrieval, Shelton CT) database. The treatment students use ST Math student accounts served by MIND. Student ST Math usage data is aggregated to grade-level means by MIND.

### 2.1 Proficiency Levels Definition

The following (Tables 1 and 2) are New Jersey’s proficiency level descriptions:

Proficiency Level	State Proficiency Level Name
L1	Partially Proficient
L2	Proficient
L3	Advanced Proficient

Table 1: NJ ASK: Proficiency Level Naming (2012/13-2013/14)

Proficiency Level	State Proficiency Level Name
L1	Did Not Yet Meet Expectations
L2	Partially Met Expectations
L3	Approached Expectations
L4	Met Expectations
L5	Exceeded Expectations

Table 2: PARCC: Proficiency Level Naming (2014/15-2015/16)

In order to compare changes in proficiency levels over time, this analysis maps the five new PARCC proficiency levels into the three old NJ ASK proficiency levels. Based on their definitions,

for 2014/15 and 2015/16, the new L1 (Partially Proficient, NJ ASK) is equal to the sum of L1 (Not Yet Meeting Expectations, PARCC), L2 (Partially Meeting Expectations, PARCC), and L3 (Approaching Expectations, PARCC). Subsequently, the new L2 (Proficient, NJ ASK) for 2014/15 and 2015/16 is equal to L4 (Meeting Expectations, PARCC) and the new L3 (Advanced Proficient, NJ ASK) is equal to L5 (Exceeding Expectations, PARCC). Moving forward, this analysis will only be comparing proficiency levels L1, L2, L3, as defined by NJ ASK.

## 2.2 Treatment Grades Pool and Selection

The Treatment grades pool originated with all schools and grades using ST Math in New Jersey. From these schools, every grade that had used the ST Math program was identified. They comprise the Treatment grades pool for this evaluation of 3-year usage.

Because the analysis uses grade-mean data, such as grade-mean scale scores or grade-mean proficiency level percentages, it is necessary that the program also be a grade-wide treatment, with the great majority of students in each grade receiving treatment. Otherwise, the grade-means reported by the state of 100% of *tested* students would not be valid measures of a smaller fraction of *treatment* students. MIND's site implementation requirement is that an entire grade, including all teachers and all classes within that grade, use the ST Math program. We validate how closely this is the case for each individual treatment grade by comparing the number of ST Math student accounts at a grade level to the New Jersey's reported enrollment at that grade level. We discard from the Treatment pool any grade with a ratio of ST Math student accounts to reported grade enrollment lower than 85%.

Furthermore, the outcomes measure is a summative year-end test, i.e. New Jersey's standardized math assessment (PARCC). The math assessment thus covers all the math standards for that entire grade level. Meanwhile, the ST Math program curriculum (arranged into Learning Objectives) is also aligned to New Jersey math standards. To infer that the ST Math content is having a valid effect on student outcomes on the summative assessment, we discard any grade with grade-mean of ST Math Progress for its students lower than 50% by year-end.

Progress is a percentage, and is defined as Levels completed by the student, divided by the total number of Levels in the grade-level curriculum. Note that student achievement of at least 50% progress in ST Math is accomplished primarily by teacher assignment of computer session time to students. With sufficient time on task, students make progress. The program helps them self-pace through providing real-time informative feedback for each puzzle.

## 2.3 Control Grades Pool and Selection

The control grades are randomly selected from a control pool of schools in New Jersey. Though they are randomly selected, they are also matched to be similar to the Treatment grades' math attributes and demographics during the baseline 2012/13 year. The matched attributes include:

- scale score
- student percentages at each math proficiency level
- percentage of students receiving free or reduced lunch (using the demographic data from MDR).



To mitigate the risk of randomly picking a set of Control grades that generates an outlier for effect, a Monte Carlo approach is used to perform many random picks. The control pool's size is large enough that there are many possible "picks" of closely matched control grades.

One hundred randomly matched picks are made and sets of matched control grades are generated. For each set, the quality of the match as well as the math growth of the potential control set is evaluated. Some picked sets have high average math growth, some have low average math growth. From the set of all picks, a median pick is chosen. This avoids either an unlikely overestimate, or underestimate, of the Control grades' growth. When multiple median picks exist, the control set with the minimal math score differences in the baseline year is chosen.

### 3 Data Analysis

The set of all schools and grades using ST Math in New Jersey is evaluated for Enrollment percentage and Progress percentage parameters. A filtered Treatment set (TRT) of all ST Math grades with  $\geq 85\%$  Enrollment and  $\geq 50\%$  Progress is identified. State math assessment data is tabulated. A matching set of Control grades based on baseline year state math assessment is selected.

Changes in math performance, i.e. the difference in math performance of a grade from a baseline year to the final year, are evaluated and tabulated. Statistical tests of the significance of the difference in math performance changes between Treatment grades and Control grades are performed. Finally, a grade-by-grade disaggregation is performed.

#### 3.1 Z-scores

When states change their state assessment throughout the years, they also change the range of possible scale scores achieved on the exam. This makes it difficult to compare changes in grade mean scale scores across years with a different exam. To deal with this issue, a new Z-score is calculated. For each year being analyzed, by grade, a Z-score takes the difference of the grade mean scale score and the mean of all scale scores statewide for that year, and then divides it by the standard deviation of all scale scores statewide for that year. Here is a fictional example to illustrate the calculation of a Z-score for the 2015/16 exam:

$$\begin{aligned} &\text{School A, Grade 3, Mean scale score: } 300 \\ &\text{Average across all schools statewide, Grade 3: } 350 \\ &\text{Standard deviation across all schools statewide, Grade 3: } 30 \\ \text{Z-score} &= ((\text{School A, Grade 3, Mean scale score}) - (\text{Average across all schools, Grade 3})) / (\text{Standard} \\ &\quad \text{deviation across all schools, Grade 3}) \\ \text{Z-score} &= \frac{300 - 350}{30} = -1.67 \end{aligned}$$

The Z-score is calculated for every grade across all years being analyzed, using the full state data set of New Jersey schools for the averages and standard deviations. The use of Z-scores is a valid statistical method to normalize any dataset and to enable analysis across otherwise uncomparable exams. In this report, we will include both mean scale scores and their accompanying Z-scores.

#### 3.2 Percentile Ranking

These newly calculated z-scores can then be converted into a percentile ranking. Each percentile ranking shows the grade's performance relative to the others in that year and grade. For example, a percentile ranking of 50 shows that this grade performed better than 50% of the grades in that testing year.

### 3.3 Final Treatment and Control

#### 3.3.1 ST Math Grade-Aggregated Implementation ( $\geq 85\%$ Enrollment Grades Only)

**ST Math Percent Grade Mean Progress Distribution – 2015/16**

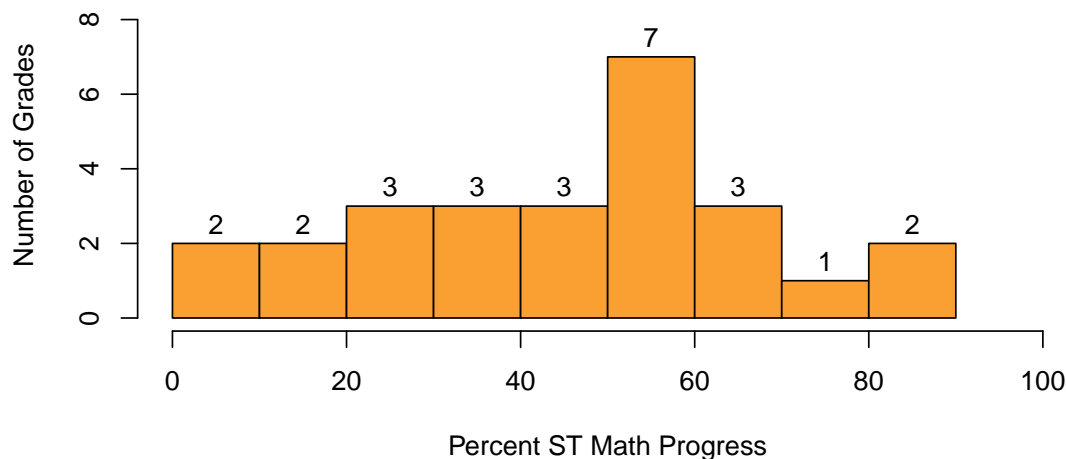


Figure 1: Histogram of ST Math Percent Progress for  $\geq 85\%$  Enrollment Grades 2015/16

For all ST Math grades with Enrollment  $\geq 85\%$ , Figure 1 shows the frequency distribution of grade-average Progress percentage through the program. Note that we will only be using grades with  $\geq 50\%$  Progress as the Treatment Group.

Table 3 provides descriptive statistics of the Progress distribution. Table 4 shows the number of remaining treatment grades after applying enrollment and progress filters.

	Min.	Max.	Average	S.D.
ST Math % Progress	5.0	87.9	44.7	22.5

Table 3: Descriptive Statistics of ST Math Percent Progress for  $\geq 85\%$  Enrollment Grades

Grades with $\geq 85\%$ Enrollment:	25
Grades with in addition $\geq 50\%$ Progress:	13

Table 4: Number of ST Math Grades with  $\geq 85\%$  Enrollment and with  $\geq 50\%$  percent progress

### 3.3.2 Filtering Treatment and Controls

Table 5 shows the total number of grades in the Treatment pool, the number of grades that exceeded the 85% Enrollment figure, and also the 50% Progress filter. Other rows in the table indicate counts of numbers of students (2015/16 from state testing count) and counts of number of schools represented. The number of matched Control (CTRL) grades, students, and schools is also shown.

	Grade 3	Grade 4	Grade 5	Total
ST Math Using Grades	9	9	8	26
ST Math Using Schools	9	9	8	10
ST Math Students	856	1346	1323	3525
ST Math Grades (Enroll $\geq$ 85%)	9	9	7	25
TRT Grades (Enroll $\geq$ 85% & Prog $\geq$ 50%)	5	4	4	13
TRT Schools (Enroll $\geq$ 85% & Prog $\geq$ 50%)	5	4	4	5
TRT Students (Enroll $\geq$ 85% & Prog $\geq$ 50%)	705	586	440	1731
CTRL Grades	5	4	4	13
CTRL Schools	5	4	4	13
CTRL Students	313	239	318	870

Table 5: Treatment Pool Filtering and Controls: Counts of Grades, Schools, and Students

### 3.3.3 Match of Controls to Treatment

Figure 2 shows the density plot of the baseline NJ ASK Math scale scores (left plot) and baseline percent students at NJ ASK Proficient or Advanced (right plot) for treatment grades overlaid on control grades, showing the closeness of the match obtained between Treatment and Control sets of grades in the baseline year, 2012/13. It is important to keep in mind that we only have a small number of treatment and control grades (13) and that the Control set was arrived at through a Monte Carlo process (see Section 2.3) rather than a closest math performance match.

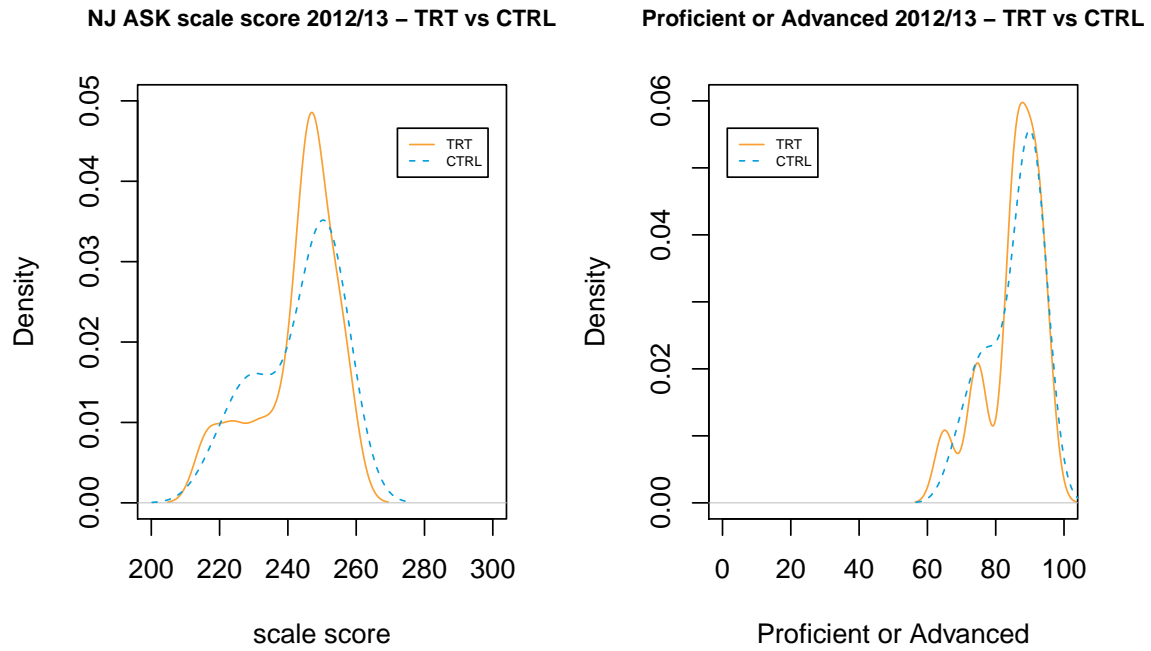


Figure 2: Baseline Year Density Plots Showing Math Scores Match between TRT and CTRL - 2012/13

Similarly, Figure 3 shows the density plot of the percentage of students needing free or reduced lunch for treatment grades overlaid on control grades, showing the closeness of the match obtained between Treatment and Control sets of grades.

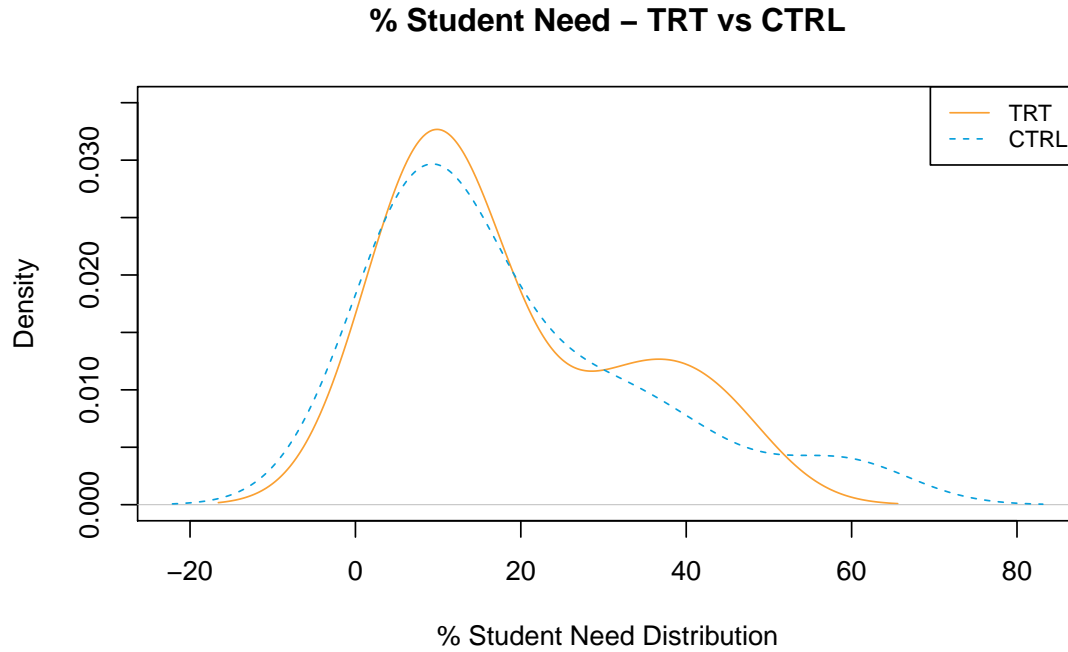


Figure 3: Baseline Year Density Plot Showing Student Need Match between TRT and CTRL

Table 6 shows the difference of the means of Treatment versus Control in the baseline year, with accompanying p-values, for percent Proficient or Advanced, for mean scale score, and for percent of students receiving free or reduced lunch. The large p-values show the differences between the Treatment and Control grades are not statistically significant.

	Mean(TRT)	SD(TRT)	Mean(CTRL)	SD(CTRL)	Estimate	P-Value
Proficient or Advanced - 2012/13	85.02	8.71	85.30	7.78	-0.28	0.93
Scale score - 2012/13	242.75	12.09	243.07	11.98	-0.32	0.95
Percent Free or Reduced Lunch	18.46	13.97	18.85	16.75	-0.38	0.95

Table 6: Matching TRT and CTRL

### 3.4 Grade-Aggregated Analysis

Table 7 shows for both Treatment (TRT) and Control (CTRL) aggregation across grades of scale scores, Z-scores, and proficiency level distributions. The far right column also shows the average ST Math Progress for the TRT set.

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Comp
TRT.12.13	13	5	1681	242.8	0.53	68.54	14.97	33.88	51.15	85.02	-
TRT.13.14	13	5	1708	241.2	0.51	68.62	16.57	34.20	49.23	83.43	66.69
TRT.14.15	13	5	1569	751.9	0.55	68.00	45.49	44.39	10.11	54.50	66.69
TRT.15.16	13	5	1606	756.5	0.52	68.23	39.48	47.76	12.72	60.48	62.83
TRT.Delta	-	-	-	513.8	-0.01	-0.31	24.52	13.88	-38.42	-24.54	-
CTRL.12.13	13	13	961	243.1	0.55	69.08	14.71	35.76	49.54	85.30	-
CTRL.13.14	13	13	912	239.9	0.45	64.77	17.13	36.91	45.93	82.84	-
CTRL.14.15	13	13	849	749.1	0.37	61.15	51.25	40.08	8.69	48.77	-
CTRL.15.16	13	13	870	754.5	0.41	63.15	43.08	43.68	13.26	56.94	-
CTRL.Delta	-	-	-	511.5	-0.14	-5.92	28.37	7.92	-36.28	-28.36	-

Table 7: Yearly Math Proficiency and Counts for TRT and CTRL Grade-Aggregated Datasets

The following chart (Figure 4) shows the changes in percentage of students at each math proficiency level for the grade-aggregated Treatment and Control sets (TRT.delta and CTRL.delta).

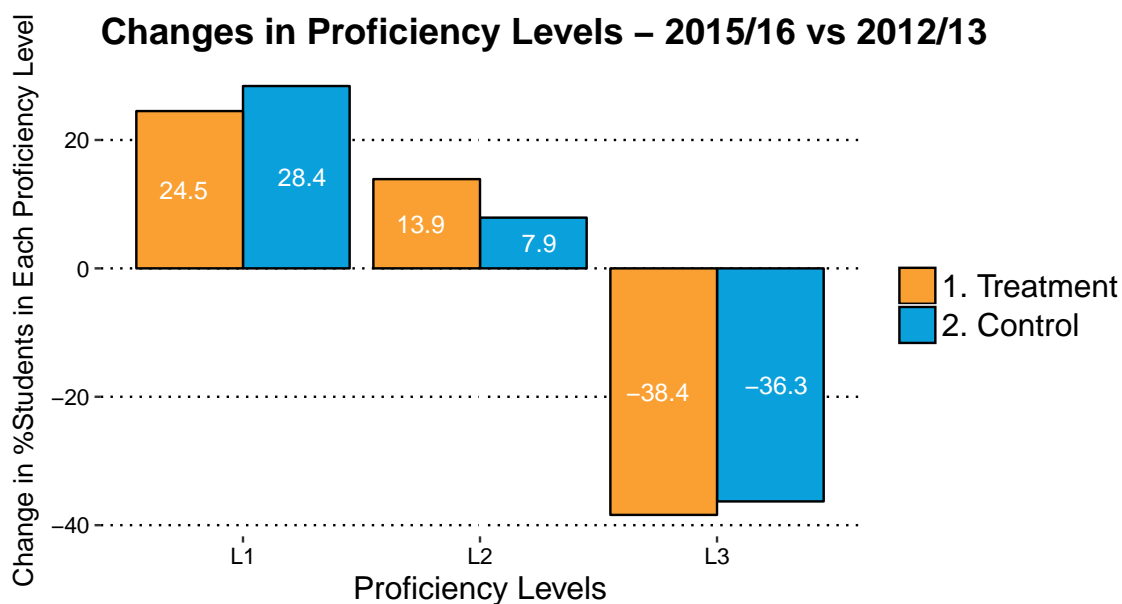


Figure 4: Change at each Proficiency Level for Grade-Aggregated TRT and CTRL Datasets between 2012/13 and 2015/16

Similarly, Figure 5 shows the changes in PARCC Math scale scores and changes in Z-scores for the grade-aggregated Treatment and Control sets.

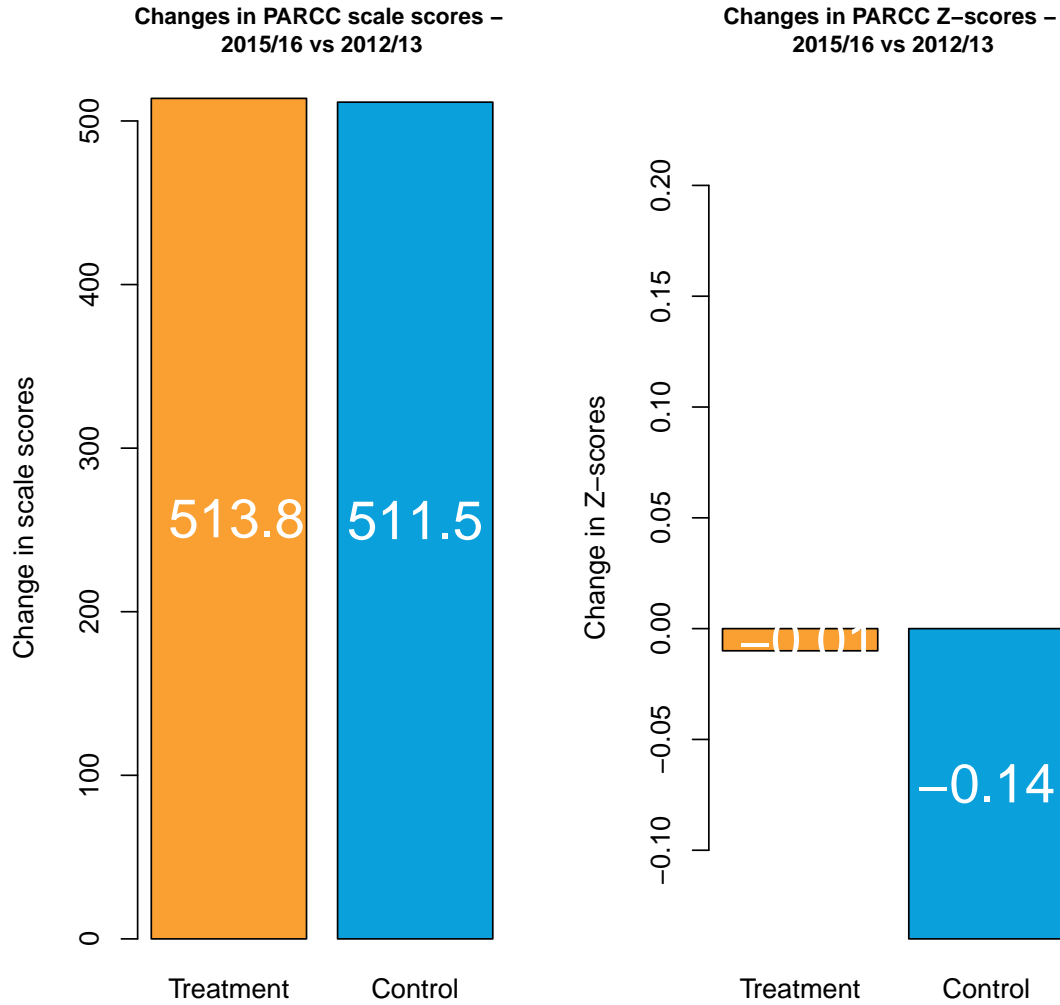


Figure 5: Changes in PARCC Math scale scores and Z-scores (See Section 3.1) for Grade-Aggregated TRT and CTRL datasets between 2012/13 and 2015/16



Further, Figure 6 shows the changes in percent of students at PARCC Met or Exceeded Expectations for the grade-aggregated Treatment and Control sets.

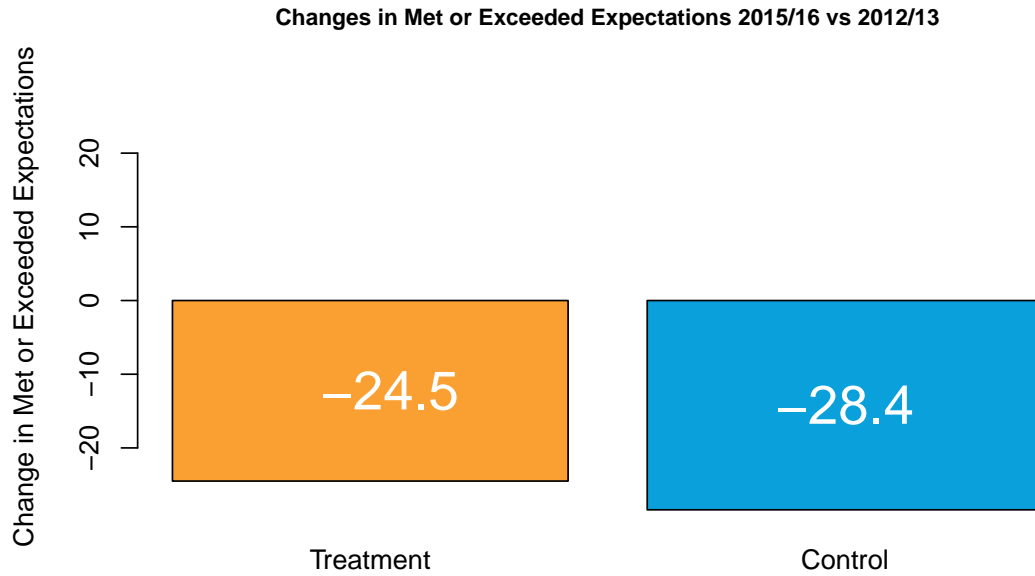


Figure 6: Changes in Met or Exceeded Expectations for Grade-Aggregated TRT and CTRL datasets between 2012/13 and 2015/16

Table 8 shows the statistics for the *differences* in changes between TRT and CTRL (Treatment - Control) for these same PARCC math proficiency and scale score changes as in the above figures.<sup>1</sup>

	Estimate	P-Value	Int.Low	Int.High
Met or Exceeded Expectations	3.82	0.43	-6.17	13.82
scale score	2.32	0.50	-4.71	9.34
Z-score	0.14	0.42	-0.21	0.48
L1	-3.85	0.43	-13.83	6.12
L2	5.97	0.35	-6.94	18.87
L3	-2.15	0.62	-10.99	6.70

Table 8: Statistics for the Differential Changes in Math Scores Growth (TRT - CTRL)

<sup>1</sup>\* statistically significant p<0.05

Finally, Figure 7 shows the changes in mean percentile ranking between TRT and CTRL.

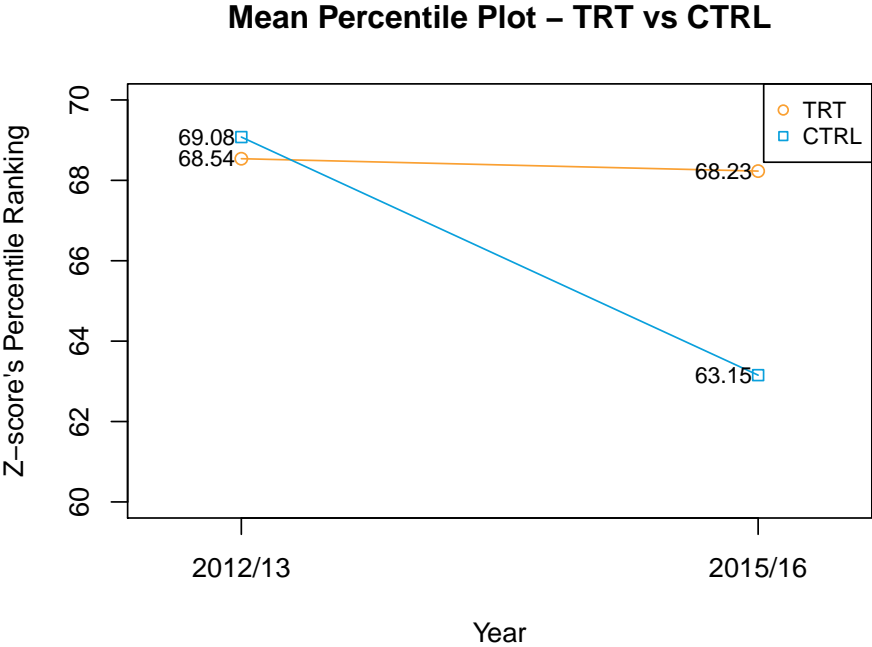


Figure 7: Changes in Percentile Ranking for TRT and CTRL Datasets between 2012/13 and 2015/16

### 3.5 Grade-Level Analysis

#### 3.5.1 Grade Level Result Tables

The following tables (Table 9, 10, and 11) present a disaggregation of results by grade level. The far right column in each table also shows the average ST Math Progress for the TRT set.

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Prog.
TRT.12.13	5	5	639	239.1	0.37	63.20	16.82	34.82	48.34	83.16	-
TRT.13.14	5	5	669	239.0	0.38	64.00	19.64	30.64	49.72	80.36	61.87
TRT.14.15	5	5	614	751.0	0.36	61.80	45.16	41.98	12.86	54.84	61.87
TRT.15.16	5	5	641	760.4	0.57	69.00	34.84	45.10	20.02	65.12	60.31
TRT.Delta	-	-	-	521.3	0.20	5.80	18.02	10.28	-28.32	-18.04	-
CTRL.12.13	5	5	360	241.4	0.47	66.80	16.40	33.94	49.68	83.62	-
CTRL.13.14	5	5	357	235.6	0.23	58.60	21.96	33.36	44.66	78.02	-
CTRL.14.15	5	5	341	747.8	0.17	55.80	51.68	40.26	8.12	48.38	-
CTRL.15.16	5	5	313	756.4	0.34	62.40	40.30	43.90	15.80	59.70	-
CTRL.Delta	-	-	-	515.0	-0.13	-4.40	23.90	9.96	-33.88	-23.92	-

Table 9: Grade 3 - Yearly Math Performance and Counts for TRT and CTRL Datasets

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Prog.
TRT.12.13	4	4	578	239.0	0.52	67.50	16.52	38.95	44.50	83.45	-
TRT.13.14	4	4	545	237.7	0.45	66.25	18.02	37.27	44.70	81.97	65.93
TRT.14.15	4	4	570	752.2	0.65	71.50	44.90	48.80	6.30	55.10	65.93
TRT.15.16	4	4	544	753.0	0.46	66.25	43.58	50.60	5.83	56.42	63.76
TRT.Delta	-	-	-	514.0	-0.06	-1.25	27.05	11.65	-38.67	-27.03	-
CTRL.12.13	4	4	261	244.6	0.80	77.00	11.65	38.75	49.65	88.40	-
CTRL.13.14	4	4	227	241.5	0.63	69.50	13.85	41.75	44.38	86.12	-
CTRL.14.15	4	4	209	750.5	0.54	67.00	51.35	38.88	9.78	48.65	-
CTRL.15.16	4	4	239	753.2	0.47	65.25	43.85	46.90	9.30	56.20	-
CTRL.Delta	-	-	-	508.7	-0.32	-11.75	32.20	8.15	-40.35	-32.20	-

Table 10: Grade 4 - Yearly Math Performance and Counts for TRT and CTRL Datasets

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Prog.
TRT.12.13	4	4	464	251.1	0.76	76.25	11.10	27.62	61.30	88.93	-
TRT.13.14	4	4	494	247.3	0.74	76.75	11.28	35.58	53.15	88.72	73.47
TRT.14.15	4	4	385	752.8	0.69	72.25	46.50	43.00	10.47	53.48	73.47
TRT.15.16	4	4	421	755.2	0.53	69.25	41.20	48.25	10.50	58.75	65.07
TRT.Delta	-	-	-	504.2	-0.22	-7.00	30.10	20.62	-50.80	-30.18	-
CTRL.12.13	4	4	340	243.7	0.41	64.00	15.65	35.05	49.25	84.30	-
CTRL.13.14	4	4	328	243.7	0.56	67.75	14.38	36.50	49.08	85.58	-
CTRL.14.15	4	4	299	749.5	0.47	62.00	50.62	41.05	8.33	49.38	-
CTRL.15.16	4	4	318	753.5	0.43	62.00	45.77	40.17	14.05	54.23	-
CTRL.Delta	-	-	-	509.8	0.02	-2.00	30.12	5.12	-35.20	-30.07	-

Table 11: Grade 5 - Yearly Math Performance and Counts for TRT and CTRL Datasets

### 3.5.2 Grade-Level Analysis of Changes in Math Met or Exceeded Expectations

Figure 8 shows the difference in the growth of percentages of students at math Met or Exceeded Expectations, for the TRT and CTRL datasets, disaggregated by grade:

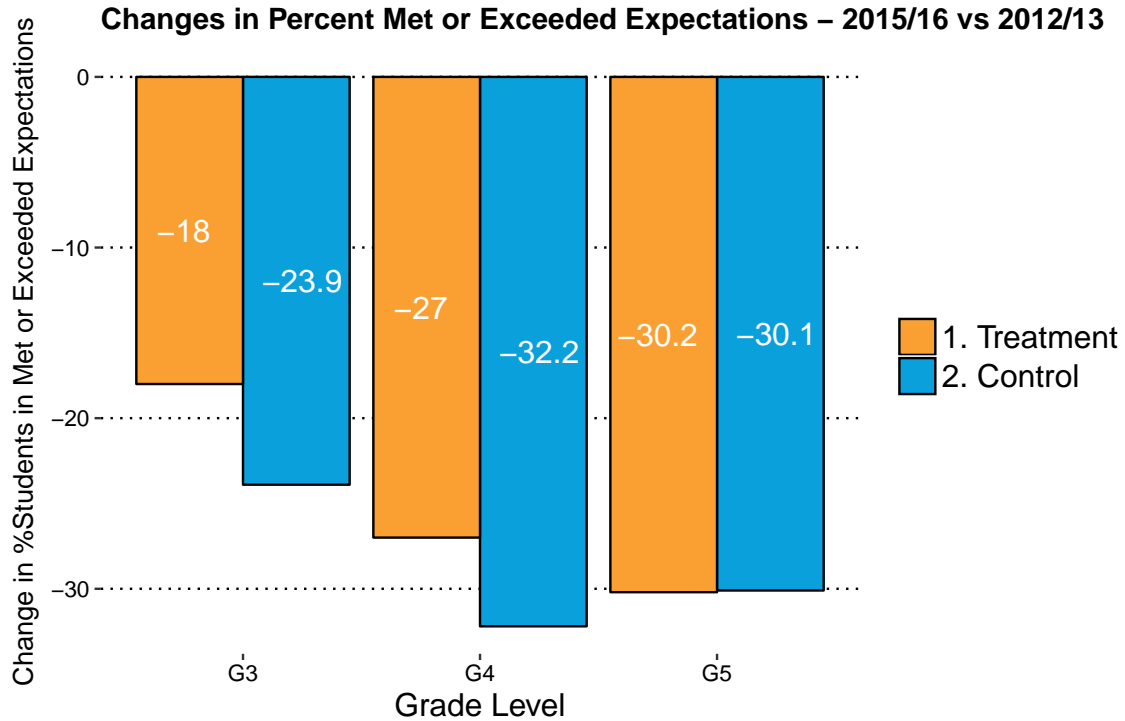


Figure 8: Changes in Percent of Students at Met or Exceeded Expectations for TRT and CTRL Datasets between 2012/13 and 2015/16

Table 12 shows the statistics for the *differences* in changes between TRT and CTRL (Treatment - Control) for these same Met or Exceeded Expectations math proficiency changes as shown in Figure 8.

	Estimate	P-Value	Int.Low	Int.High
Grade 3	5.88	0.32	-6.81	18.57

Table 12: Statistics for the Differential Changes in Met or Exceeded Expectations, (TRT - CTRL)

### 3.5.3 Grade-Level Analysis of Changes in PARCC Math scale scores

Figure 9 shows the changes in the grade-mean math scale scores of students for the TRT and CTRL datasets, disaggregated by grade:

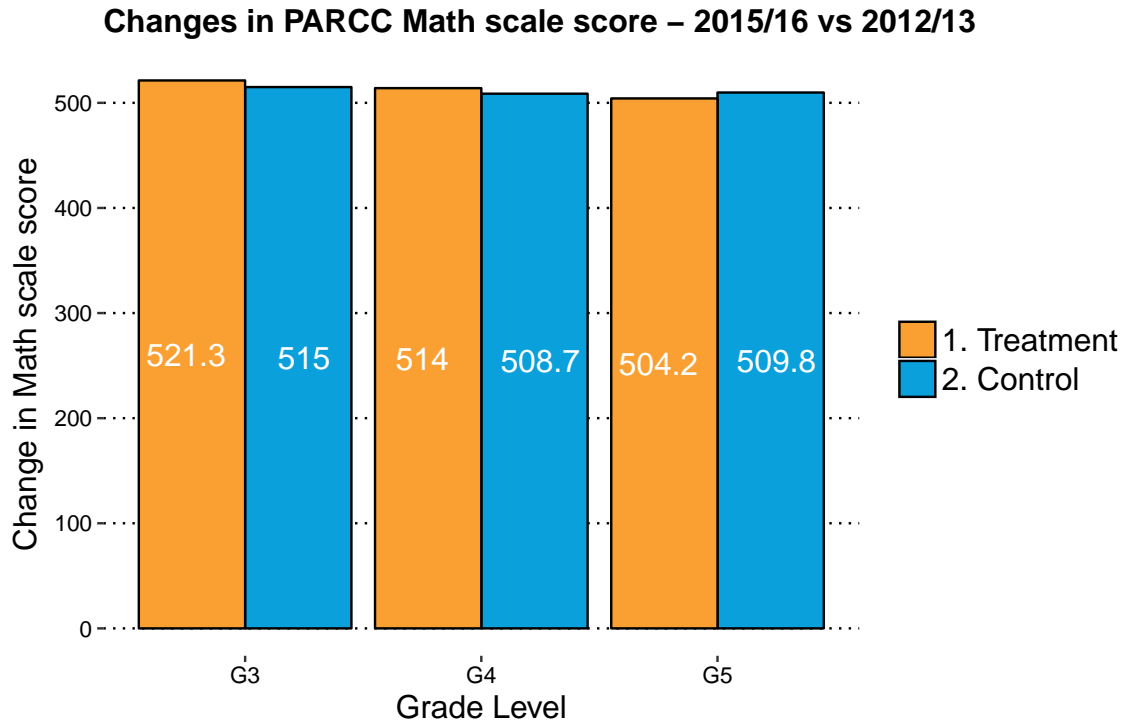


Figure 9: Changes in Grade-Mean PARCC Math scale score for TRT and CTRL Datasets between 2012/13 and 2015/16

Table 13 shows the statistics for the differences between TRT and CTRL (Treatment - Control) for these same PARCC math scale score changes as shown in Figure 9.

	Estimate	P-Value	Int.Low	Int.High
Grade 3	6.30	0.05*	0.16	12.44

Table 13: Statistics for the Differential Changes in PARCC Math scale scores Growth, (TRT - CTRL)

### 3.5.4 Grade-Level Analysis of Changes in PARCC Z-scores of scale scores

Figure 10 shows the changes in the grade-mean Z-scores of students for the TRT and CTRL datasets, disaggregated by grade:

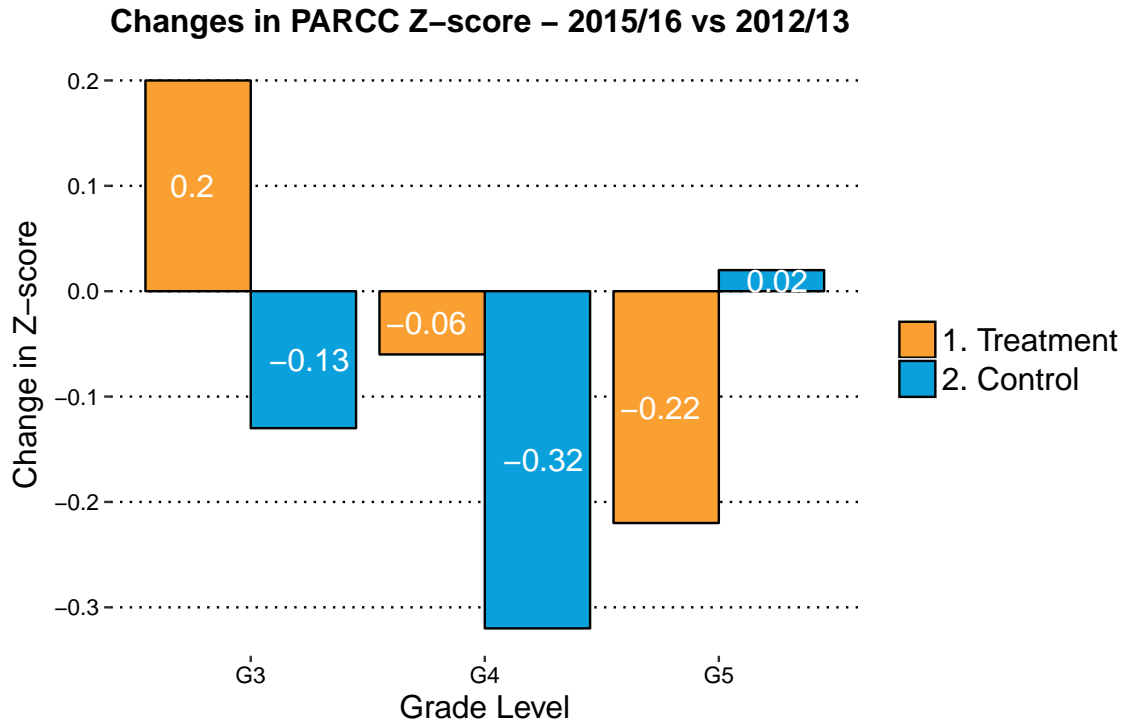


Figure 10: Changes in Grade-Mean PARCC Z-score (See Section 3.1) for TRT and CTRL Datasets between 2012/13 and 2015/16

Table 14 shows the statistics for the differences between TRT and CTRL (Treatment - Control) for these same PARCC Z-score changes as shown in Figure 10.

	Estimate	P-Value	Int.Low	Int.High
Grade 3	0.33	0.09	-0.06	0.72

Table 14: Statistics for the Differential Changes in PARCC Z-scores (See Section 3.1) Growth, (TRT - CTRL)

## 4 Effect Size

The following table shows the effect sizes for Met or Exceeded Expectations, PARCC scale score, and accompanying Z-score.

	Scale score Effect Size	Z-score Effect Size	Met or Exceeded Expectations Effect Size
Grade 3	0.53	0.61	0.76
Grade 4	0.58	0.57	0.84
Grade 5	-0.33	-0.30	-0.01
All Grades	0.19	0.23	0.49

Table 15: Cohen’s d Effect Size

## 5 Findings Summary

New Jersey grades 3, 4, and 5 using ST Math for the year 2015/16 averaged 44.7% ST Math Progress. 13/26 grades (50%) averaged covering more than 50% of ST Math content. A statistically significant difference was found in this analysis for individual grade levels. Looking at Table 13, a statistically significant difference was found for grade 3 PARCC scale score, with an estimate of 6.3 in favor of the ST Math treatment set.

## 6 Confounders

Despite best efforts in minimizing confounders to the results of this analysis, there still remain a few input variables that could be significant in affecting differences of state test score outcomes between the Treatment and Control sets. One issue is the lack of randomization of grades chosen to receive the ST Math treatment. Instead of randomized selection, Treatment grades are self-selected. Self-selection can be an indication of districts or schools with a focus on math, an appetite for change, and with a spotlight on math training. Furthermore, not all grades using the ST Math program are chosen for analysis. Each grade must pass two specific filters to be considered for the Treatment set: the first being an enrollment filter of at least 85% of students in each grade using the program, and the second being a progress filter of at least 50% of the program completed on average by students in that grade. These filters might indicate relatively high-functioning schools with a team of relatively effective teachers in that grade, thus resulting in better instruction overall. A mitigation of this possible confounder is our selection of treatment groups on the grade level, rather than the teacher level, so there is no cherry picking of teachers: the full range of teachers in each grade is included. Moreover, the specific teachers may often be the same in the baseline year as in the current year, so the Treatment growth is not due to teacher differences. Finally, a possible confounder lies in the “business as usual” conditions at the matched control grades chosen for each analysis. It’s unknown whether these control grades used other programs that could affect the comparison of the two sets of grades. The Monte Carlo Method is used to mitigate the possibility of control picks being favorable or unfavorable (see Section 2.3).

## 7 Reference Tables Grouped By School Year

The following tables show grade-level details, grouped by school year and for treatment (Table 16) and controls (Table 17) separately.

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Comp.
Grade 3 (12.13)	5	5	639	239.1	0.37	63.2	16.82	34.82	48.34	83.16	-
Grade 4 (12.13)	4	4	578	239.0	0.52	67.50	16.52	38.95	44.50	83.45	-
Grade 5 (12.13)	4	4	464	251.1	0.76	76.25	11.10	27.62	61.30	88.93	-
All Grades (12.13)	13	5	1681	242.8	0.53	68.54	14.97	33.88	51.15	85.02	-
Grade 3 (13.14)	5	5	669	239.0	0.38	64.0	19.64	30.64	49.72	80.36	61.87
Grade 4 (13.14)	4	4	545	237.7	0.45	66.25	18.02	37.27	44.70	81.97	65.93
Grade 5 (13.14)	4	4	494	247.3	0.74	76.75	11.28	35.58	53.15	88.72	73.47
All Grades (13.14)	13	5	1708	241.2	0.51	68.62	16.57	34.20	49.23	83.43	66.69
Grade 3 (14.15)	5	5	614	751.0	0.36	61.8	45.16	41.98	12.86	54.84	61.87
Grade 4 (14.15)	4	4	570	752.2	0.65	71.50	44.90	48.80	6.30	55.10	65.93
Grade 5 (14.15)	4	4	385	752.8	0.69	72.25	46.50	43.00	10.47	53.48	73.47
All Grades (14.15)	13	5	1569	751.9	0.55	68.00	45.49	44.39	10.11	54.50	66.69
Grade 3 (15.16)	5	5	641	760.4	0.57	69.0	34.84	45.10	20.02	65.12	60.31
Grade 4 (15.16)	4	4	544	753.0	0.46	66.25	43.58	50.60	5.83	56.42	63.76
Grade 5 (15.16)	4	4	421	755.2	0.53	69.25	41.20	48.25	10.50	58.75	65.07
All Grades (15.16)	13	5	1606	756.5	0.52	68.23	39.48	47.76	12.72	60.48	62.83

Table 16: TRT Grades Detail Sorted by Year

	# Grades	# Schools	# Students	Scale score	Z-score	Percentile	L1	L2	L3	Met or Exceeded Expectations	ST Math Per Comp.
Grade 3 (12.13)	5	5	360	241.4	0.47	66.8	16.40	33.94	49.68	83.62	-
Grade 4 (12.13)	4	4	261	244.6	0.80	77.00	11.65	38.75	49.65	88.40	-
Grade 5 (12.13)	4	4	340	243.7	0.41	64.00	15.65	35.05	49.25	84.30	-
All Grades (12.13)	13	13	961	243.1	0.55	69.08	14.71	35.76	49.54	85.30	-
Grade 3 (13.14)	5	5	357	235.6	0.23	58.6	21.96	33.36	44.66	78.02	-
Grade 4 (13.14)	4	4	227	241.5	0.63	69.50	13.85	41.75	44.38	86.12	-
Grade 5 (13.14)	4	4	328	243.7	0.56	67.75	14.38	36.50	49.08	85.58	-
All Grades (13.14)	13	13	912	239.9	0.45	64.77	17.13	36.91	45.93	82.84	-
Grade 3 (14.15)	5	5	341	747.8	0.17	55.8	51.68	40.26	8.12	48.38	-
Grade 4 (14.15)	4	4	209	750.5	0.54	67.00	51.35	38.88	9.78	48.65	-
Grade 5 (14.15)	4	4	299	749.5	0.47	62.00	50.62	41.05	8.33	49.38	-
All Grades (14.15)	13	13	849	749.1	0.37	61.15	51.25	40.08	8.69	48.77	-
Grade 3 (15.16)	5	5	313	756.4	0.34	62.4	40.30	43.90	15.80	59.70	-
Grade 4 (15.16)	4	4	239	753.2	0.47	65.25	43.85	46.90	9.30	56.20	-
Grade 5 (15.16)	4	4	318	753.5	0.43	62.00	45.77	40.17	14.05	54.23	-
All Grades (15.16)	13	13	870	754.5	0.41	63.15	43.08	43.68	13.26	56.94	-

Table 17: CTRL Grades Detail Sorted by Year



## 8 Lists of Schools

### 8.1 Treatment Schools

The following table lists the treatment schools and grades (after 85% enrollment and 50% progress filtering) used in the analysis.

PID	IID	District	School Name	GRADE
666721	WAR0MB	HAMMONTON TOWN	WARREN E. SOOY JR. ELEMENTARY SCHOOL	3, 4
679584	JEF0JK	SOUTH ORANGE-MAPLEWOOD	JEFFERSON ELEMENTARY SCHOOL	3, 4, 5
679651	SET0JK	SOUTH ORANGE-MAPLEWOOD	SETH BOYDEN ELEMENTARY DEMONSTRATION SCHOOL	3, 5
679637	SOU0JN	SOUTH ORANGE-MAPLEWOOD	SOUTH MOUNTAIN ELEMENTARY/ANNEX	3, 4, 5
679663	TUS0JK	SOUTH ORANGE-MAPLEWOOD	TUSCAN ELEMENTARY	3, 4, 5

Table 18: Treatment Schools (TRT Dataset)

## 8.2 Control Schools

The following table lists the control schools and grades (matched control grades to treatment grades) used in the analysis.

PID	District	School Name	GRADE
700949	BERKELEY HEIGHTS TWP	WILLIAM WOODRUFF SCHOOL	4
688626	EAST BRUNSWICK TWP	FROST ELEMENTARY SCHOOL	5
674261	LAUREL SPRINGS BORO	LAUREL SPRINGS SCHOOL	4
676594	LAWRENCE TWP	MYRON L. POWELL ELEMENTARY SCHOOL	5
700614	NEWTON TOWN	MERRIAM AVENUE SCHOOL	3
692512	OCEAN TWP	WAYSIDE ELEMENTARY SCHOOL	3
694651	PARSIPPANY-TROY HILLS TWP	TROY HILLS ELEMENTARY SCHOOL	3
690148	SOUTH BRUNSWICK TWP	BROOKS CROSSING ELEMENTARY SCHOOL	5
690112	SOUTH BRUNSWICK TWP	CONSTABLE ELEMENTARY SCHOOL	4
702301	SUMMIT CITY	BRAYTON ELEMENTARY SCHOOL	4
4813548	TEANECK COMMUNITY CS	TEANECK COMMUNITY CHARTER SCHOOL	3
674819	VOORHEES TWP	EDWARD T. HAMILTON	3
690502	WOODBIDGE TWP	MATTHEW JAGO ELEMENTARY SCHOOL	5

Table 19: Matched Control Schools (CTRL Dataset)